Blind (Uninformed) Search

(Where we systematically explore alternatives)

R&N: Chap. 3, Sect. 3.3-5

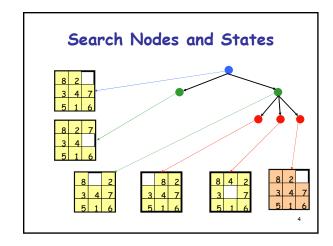
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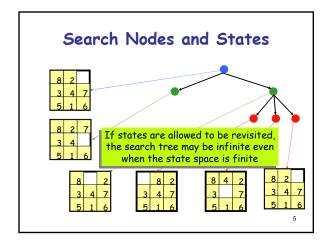
Simple Problem-Solving-Agent Agent Algorithm

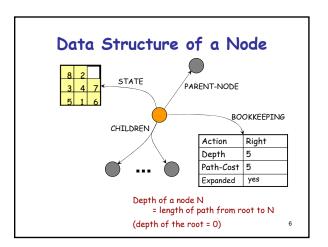
- 1. $s_0 \leftarrow \text{sense/read initial state}$
- 2. GOAL? ← select/read goal test
- 3. Succ ← read successor function
- 4. solution \leftarrow search(s₀, GOAL?, Succ)
- perform(solution)

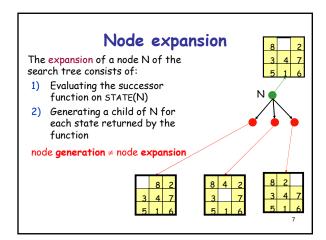
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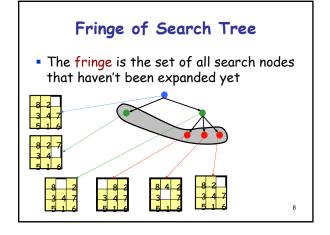
Search Tree Search Tree State graph Note that some states may be visited multiple times

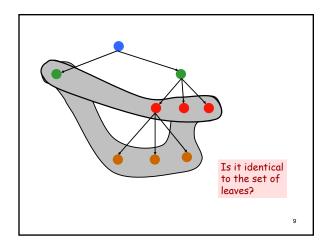












Search Strategy

- The fringe is the set of all search nodes that haven't been expanded yet
- The fringe is implemented as a priority queue FRINGE
 - INSERT(node,FRINGE)
 - REMOVE(FRINGE)
- The ordering of the nodes in FRINGE defines the search strategy

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Search Algorithm #1

SEARCH#1

- 1. If GOAL?(initial-state) then return initial-state
- 2. INSERT(initial-node,FRINGE)
- 3. Repeat:
 - a. If empty(FRINGE) then return failure
 - b. N ← REMOVE(FRINGE)
 - c. s ← STATE(N)
 - d. For every state s' in SUCCESSORS(s)
 - i. Create a new node N' as a child of N
 - ii. If GOAL?(s') then return path or goal state
 - iii. INSERT(N',FRINGE)

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Expansion of N

Performance Measures

Completeness

A search algorithm is complete if it finds a solution whenever one exists

[What about the case when no solution exists?]

Optimality

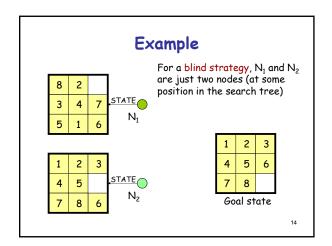
A search algorithm is optimal if it returns a minimum-cost path whenever a solution exists

Complexity

It measures the time and amount of memory required by the algorithm

Blind vs. Heuristic Strategies

- Blind (or un-informed) strategies do not exploit state descriptions to order FRINGE. They only exploit the positions of the nodes in the search tree
- Heuristic (or informed) strategies exploit state descriptions to order FRINGE (the most "promising" nodes are placed at the beginning of FRINGE)



Remark

• Some search problems, such as the (n²-1)-

One can't expect to solve all instances of

One may still strive to solve each instance

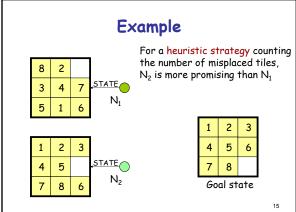
→ This is the purpose of the search strategy

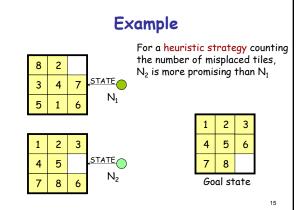
such problems in less than exponential

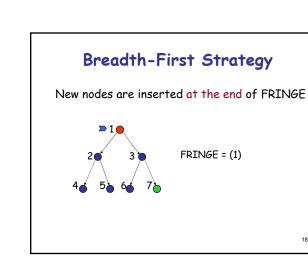
puzzle, are NP-hard

as efficiently as possible

time (in n)

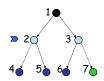






Breadth-First Strategy

New nodes are inserted at the end of FRINGE

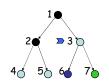


FRINGE = (2, 3)

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Breadth-First Strategy

New nodes are inserted at the end of FRINGE

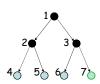


FRINGE = (3, 4, 5)

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Breadth-First Strategy

New nodes are inserted at the end of FRINGE



FRINGE = (4, 5, 6, 7)

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Important Parameters

- 1) Maximum number of successors of any state
 - \rightarrow branching factor b of the search tree
- 2) Minimal length (\neq cost) of a path between the initial and a goal state
 - → depth d of the shallowest goal node in the search tree

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Evaluation

- b: branching factor
- d: depth of shallowest goal node
- Breadth-first search is:
 - · Complete? Not complete?
 - · Optimal? Not optimal?

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Evaluation

- b: branching factor
- d: depth of shallowest goal node
- Breadth-first search is:
 - · Complete
 - Optimal if step cost is 1
- Number of nodes generated:

Evaluation

- b: branching factor
- d: depth of shallowest goal node
- Breadth-first search is:
 - Complete
 - · Optimal if step cost is 1
- Number of nodes generated:

 $1 + b + b^2 + ... + b^d = ???$

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Evaluation

- b: branching factor
- d: depth of shallowest goal node
- Breadth-first search is:
 - Complete
 - · Optimal if step cost is 1
- Number of nodes generated:

 $1 + b + b^2 + ... + b^d = (b^{d+1}-1)/(b-1) = O(b^d)$

• \rightarrow Time and space complexity is $O(b^d)$

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Big O Notation

g(n) = O(f(n)) if there exist two positive constants a and N such that:

for all n > N: $g(n) \le a \times f(n)$

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Time and Memory Requirements

| d | # Nodes | Time | Memory |
|----|---------|-----------|---------------|
| 2 | 111 | .01 msec | 11 Kbytes |
| 4 | 11,111 | 1 msec | 1 Mbyte |
| 6 | ~106 | 1 sec | 100 Mb |
| 8 | ~108 | 100 sec | 10 Gbytes |
| 10 | ~1010 | 2.8 hours | 1 Tbyte |
| 12 | ~1012 | 11.6 days | 100 Tbytes |
| 14 | ~1014 | 3.2 years | 10,000 Tbytes |

Assumptions: b = 10; 1,000,000 nodes/sec; 100bytes/node

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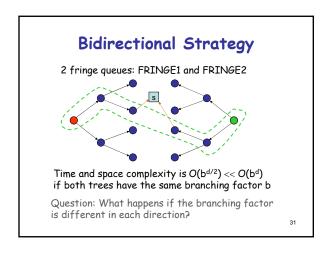
Remark

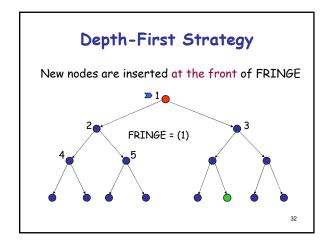
If a problem has no solution, breadth-first may run for ever (if the state space is infinite or states can be revisited arbitrary many times)

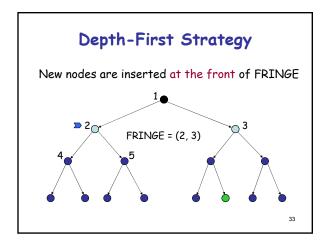
| 1 | 2 | 3 | 4 |
|----|----|----|----|
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | |

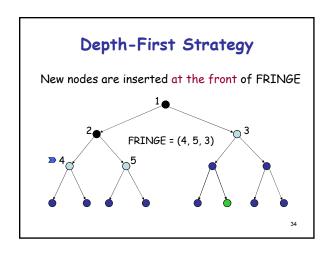


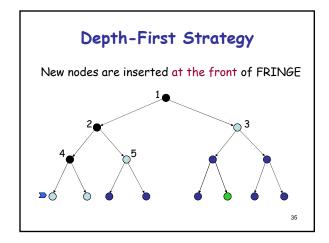
| 1 | 2 | 3 | 4 |
|----|----|----|----|
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 15 | 14 | |

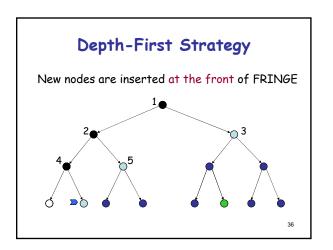


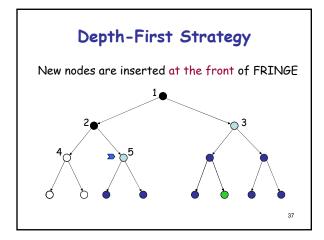


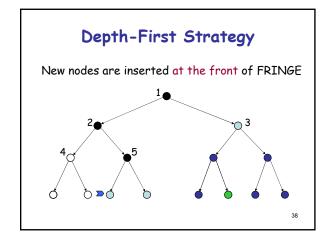


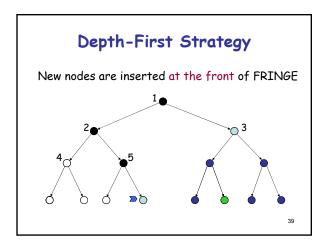


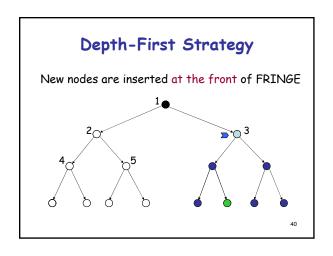


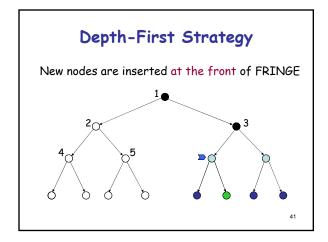


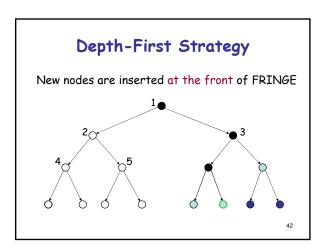












Evaluation

- b: branching factor
- d: depth of shallowest goal node
- m: maximal depth of a leaf node
- Depth-first search is:
 - Complete?
 - Optimal?

Evaluation

- b: branching factor
- d: depth of shallowest goal node
- m: maximal depth of a leaf node
- Depth-first search is:
 - Complete only for finite search tree
 - Not optimal
- Number of nodes generated (worst case): $1 + b + b^2 + ... + b^m = O(b^m)$
- Time complexity is O(b^m)
- Space complexity is O(bm) [or O(m)]

[Reminder: Breadth-first requires $O(b^d)$ time and space]

Depth-Limited Search

- Depth-first with depth cutoff k (depth at which nodes are not expanded)
- Three possible outcomes:
 - Solution
 - · Failure (no solution)
 - Cutoff (no solution within cutoff)

Iterative Deepening Search

Provides the best of both breadth-first and depth-first search

Totally horrifying! Main idea:

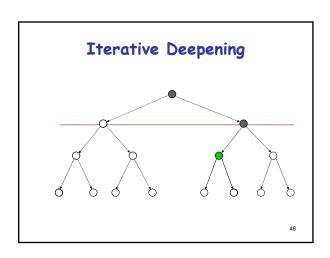
IDS

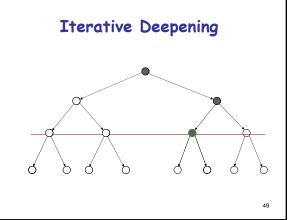
For k = 0, 1, 2, ... do:

Perform depth-first search with depth cutoff k

(i.e., only generate nodes with depth $\leq k$)

Iterative Deepening





Performance

- Iterative deepening search is:
 - Complete
 - Optimal if step cost =1
- Time complexity is: $(d+1)(1) + db + (d-1)b^2 + ... + (1) b^d = O(b^d)$
- Space complexity is: O(bd) or O(d)

0

Calculation

$$db + (d-1)b^{2} + ... + (1) b^{d}$$

$$= b^{d} + 2b^{d-1} + 3b^{d-2} + ... + db$$

$$= (1 + 2b^{-1} + 3b^{-2} + ... + db^{-d}) \times b^{d}$$

$$\leq (\sum_{i=1}^{n} b^{(i-i)}) \times b^{d} = b^{d} (b/(b-1))^{2}$$

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Number of Generated Nodes (Breadth-First & Iterative Deepening)

d = 5 and b = 2

| BF | ID |
|----|-------------|
| 1 | 1 × 6 = 6 |
| 2 | 2 x 5 = 10 |
| 4 | 4 × 4 = 16 |
| 8 | 8 × 3 = 24 |
| 16 | 16 x 2 = 32 |
| 32 | 32 x 1 = 32 |
| 63 | 120 |

120/63 ~ 2

E2

Number of Generated Nodes (Breadth-First & Iterative Deepening)

d = 5 and b = 10

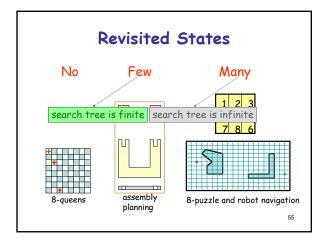
| BF | ID |
|---------|---------|
| 1 | 6 |
| 10 | 50 |
| 100 | 400 |
| 1,000 | 3,000 |
| 10,000 | 20,000 |
| 100,000 | 100,000 |
| 111,111 | 123,456 |

123,456/111,111 ~ 1.111

Comparison of Strategies

- Breadth-first is complete and optimal, but has high space complexity
- Depth-first is space efficient, but is neither complete, nor optimal
- Iterative deepening is complete and optimal, with the same space complexity as depth-first and almost the same time complexity as breadth-first

Quiz: Would IDS + bi-directional search be a good combination?



Avoiding Revisited States

- Requires comparing state descriptions
- Breadth-first search:
 - Store all states associated with generated nodes in VISITED
 - If the state of a new node is in VISITED, then discard the node

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Avoiding Revisited States

- Requires comparing state descriptions
- Breadth-first search:
 - Store all states associated with generated nodes in VISITED
 - If the state of a new node is in VISITED, then discard the node

Implemented as hash-table or as explicit data structure with flags

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Avoiding Revisited States

Depth-first search:

Solution 1:

- Store all states associated with nodes in current path in VISITED
- If the state of a new node is in VISITED, then discard the node

→ >>

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Avoiding Revisited States

Depth-first search:

Solution 1:

- Store all states associated with nodes in current path in VISITED
- If the state of a new node is in VISITED, then discard the node
- → Only avoids loops

Solution 2:

- Store all generated states in VISITED
- If the state of a new node is in VISITED, then discard the node
- → Same space complexity as breadth-first!

Uniform—Cost Search

• Each arc has some cost $c \ge \varepsilon > 0$ • The cost of the path to each node N is $g(N) = \Sigma$ costs of arcs
• The goal is to generate a solution path of minimal cost
• The nodes N in the queue FRINGE are sorted in increasing g(N)

Search Algorithm #2

SEARCH#2

1. INSERT(initial-node,FRINGE)

2. Repeat:

The goal test is applied to a node when this node is **expanded**, not when it is generated.

- a. If empty(FRINGE) then return failure
- b. $N \leftarrow REMOVE(FRINGE)$
- c. s ← STATE(N)
- \rightarrow d. If GOAL?(s) then return path or goal state
 - e. For every state s' in SUCCESSORS(s)
 - i. Create a node N' as a successor of N
 - ii. INSERT(N',FRINGE)

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Avoiding Revisited States in Uniform-Cost Search

- For any state S, when the first node N such that STATE(N) = S is expanded, the path to N is the best path from the initial state to S
- So:
 - When a node is expanded, store its state into CLOSED
 - When a new node N is generated:
 - If STATE(N) is in CLOSED, discard N
 - If there exits a node N' in the fringe such that STATE(N') = STATE(N), discard the node N or N' with the highest-cost path $_{62}$